

# Image Data Compression

## Introduction to watermarking and steganography

# Examples and common terminology

## Example: watermarks (WMs) embedded in paper money

- Hidden from view (or non-obstructing) in normal use
- Recovered via a special process (holding up to light)
- Contains information related to object (bill authenticity)
- The presence of a watermark may be known to user

## Example: a secret message written with milk on top of a non-secret (cover, or decoy) letter written with ink

- Hidden message is unrelated to the “decoy” letter
- The presence of the hidden message itself is secret (otherwise called “overt embedded communication”)
- From Greek “steganos” = “covered”

## Watermarking of electronic signals:

**Work:** a specific signal, such as an image, audio or video record (e.g., song in MP3)

**Content:** set of all Works (e.g., all audio music) that may be WM'ed

**Medium:** means of representing, transmitting or recording the content (e.g., a CD)

**Cover Work:** original signal before modification (called message *embedding*)

Book on subject:  
[Cox et al, '08]

**Watermarking:** *imperceptibly* altering a Work to embed a message **about that Work**

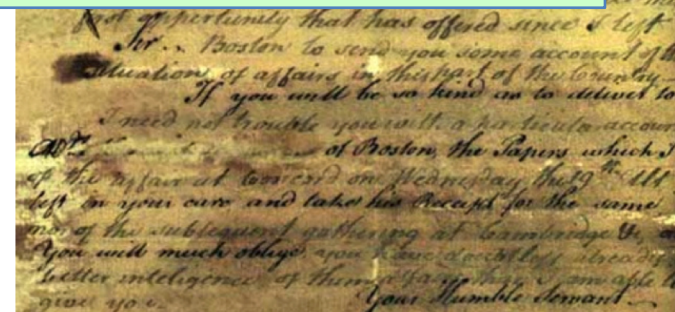
**Steganography:** *undetectedly* altering a Work to embed a **secret message**

**Steganalysis:** detection *whether* secret steganographic communication is taking place

## Watermarking

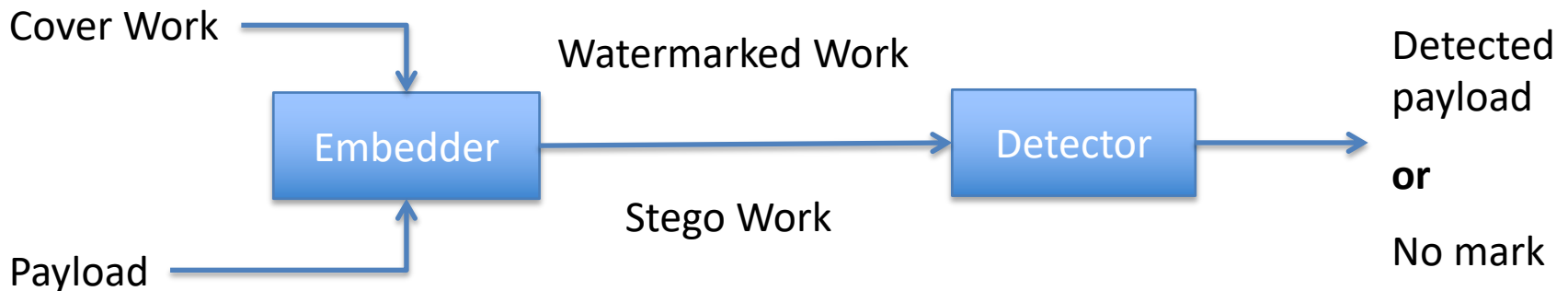


## Steganographic communication



# Categorization of information hiding

	Cover Work-dependent message	Cover Work-independent message
Existence of message is hidden	<b>Covert watermarking</b> <b>Example:</b> In 1981, M. Thatcher marked copies of secret documents with unique word spacing patterns to find a cabinet minister who had leaked information.	<b>Steganography</b> <b>Example:</b> SALT-II nuclear treaty described sensors on missile silos, reporting if a silo is occupied. Both USSR and USA investigated if sensors could transmit other information.
Existence of message is known	<b>Overt watermarking</b> <b>Example:</b> Web-sites of some museums provide high-quality digital images of the collection, with a warning that each image is watermarked to protect it against piracy or reproduction.	<b>Overt embedded communication</b> <b>Example:</b> In late 1940s, a time code at 800Hz frequency was embedded in radio broadcast. The code was inaudible, and only communicated the current time to various automatic devices.



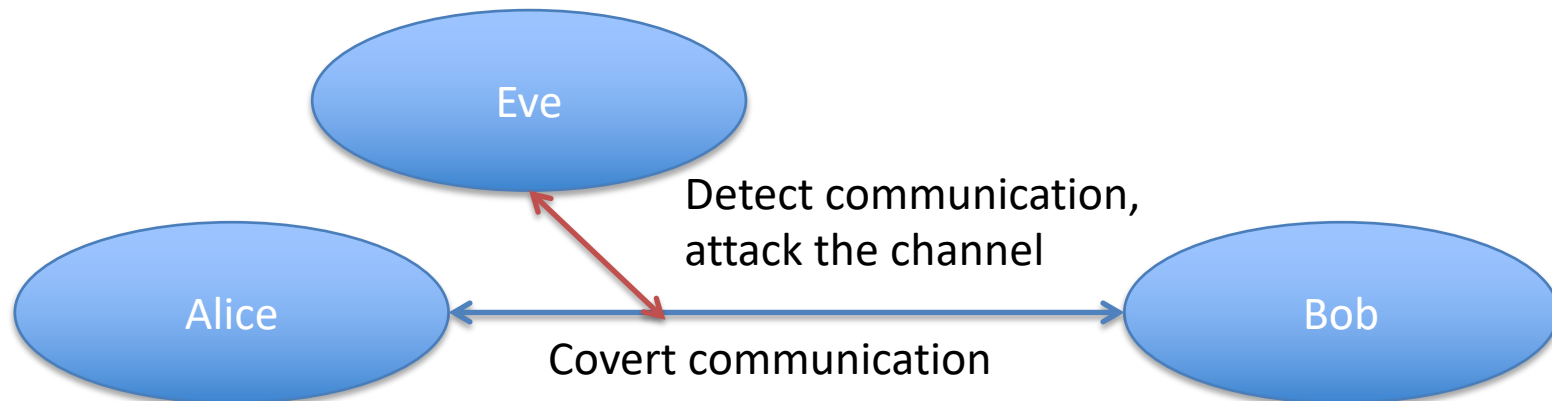
# Possible uses of digital watermarking and steganography

## Watermarking:

- Internet and high-capacity digital recording devices facilitate unauthorized copying
- Cryptography provides the protection in transit, but not after delivery
- Watermarking is a complement to cryptographic protection, never removed during use, may be designed to survive content transformations (re-encoding, format changes, etc.)

## Steganography:

- Electronic communications are susceptible to eavesdropping and interventions
- Security and privacy can be addressed by cryptographic tools, or by anonymous remailers
- However, encryption is not hidden, and the presence of the communication is obvious
- Steganography can be used also in cases when the message encryption is prohibited
- Cryptanalysis aims to establish whether communication is taking place (e.g. to prevent criminal activities or to identify members of an organization)



# Some specific applications of digital watermarking

- Broadcast monitoring
  - air time verification, re-broadcasting control, ads control
  - active vs passive monitoring: index complexity reduction
- Owner identification
  - legal copyright notice, owner contact information
- Proof of ownership
  - key in central repository, digital “negative”, asymmetric identification of original / derived work
- Transaction tracking (fingerprinting of copies)
  - e.g. identification of leaking party at Oscar Award previews
- Content authentication
  - tampering detection, localized [semi]fragile digital signature
- Copy / Record / Playback control
  - e.g. DVD copy protection
- Device control
  - copy prevention marks, ads indicator, traffic info on FM radio
- Legacy enhancement
  - digital signals over analog networks, lyrics in MP3

## Desired WM properties and characteristics:

- Imperceptibility: WM must not ruin the aesthetics of Cover Work
- Inseparability: WM cannot be removed by converting, re-formatting, etc.



Example of (relatively poor) watermarking as owner identification: the complete Lena image and its (usually omitted) copyright notice



# Quantitative metrics of watermarking systems

- **Embedding effectiveness**
  - probability that output is identified as watermarked immediately after embedding (may be <100%)
  - compromise between effectiveness and fidelity; determined analytically or with large DB of Works
- **Fidelity**
  - how imperceptible WM is in Work; perceptual similarity between original and watermarked Works (possibly after additional degradation of both due to delivery); based on some perceptive model
- **Robustness**
  - how well WM survives common signal processing operations: spatial / temporal filtering, lossy compression, printing / scanning, geometric distortions etc.
- **Data payload**
  - number of bits a watermark encodes per unit of time or per Work;
  - N-bit WM encodes  $2^N+1$  possible detector outputs (one bit always encodes very presence of WM)
- **Blind [public] or informed [private] detection**
  - whether original Work is needed for successful detection
- **False positive rate**
  - probability to erroneously detect a missing WM per detector run (fixed Work, random WMs)
- **Security**
  - ability to resist hostile attacks, such as unauthorized removal (elimination, masking, collusion) / embedding (forgery) = active attacks, unauthorized detection = passive attack
- **Use of secret watermark key (similar to cipher key)**
- **Cost**
  - deployment of embedders / detectors, computational load, real-time requirements etc.

# Properties of steganographic and steganalytic systems

## Recall the primary goal of steganography:

conceal the fact that the covert communication is present within innocuous communication

## Properties of a WM system irrelevant for steganography:

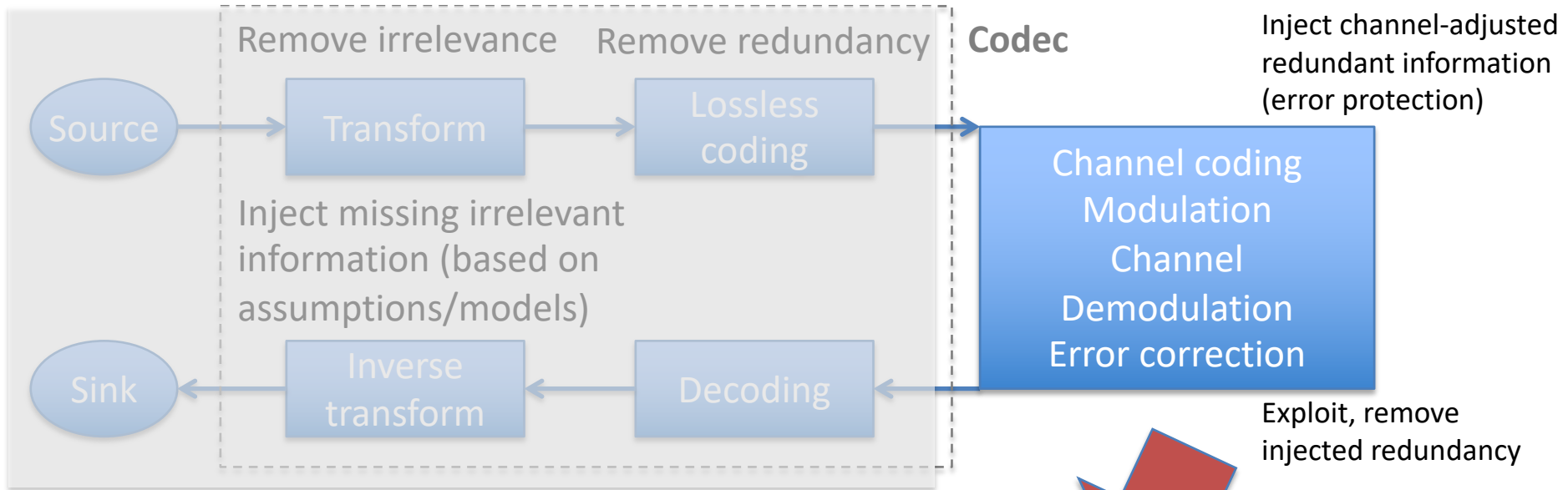
- **Embedding effectiveness:** N/A, due to freedom to choose a suitable Cover Work
- **Fidelity:** N/A, since the steganalyzing party normally has no access to the original Work
- **Blind / informed extraction:** N/A, one usually assumes that the original Work is not available
- **Robustness:** N/A, noise etc. not a big issue for modern digital communication

## Properties important for steganography:

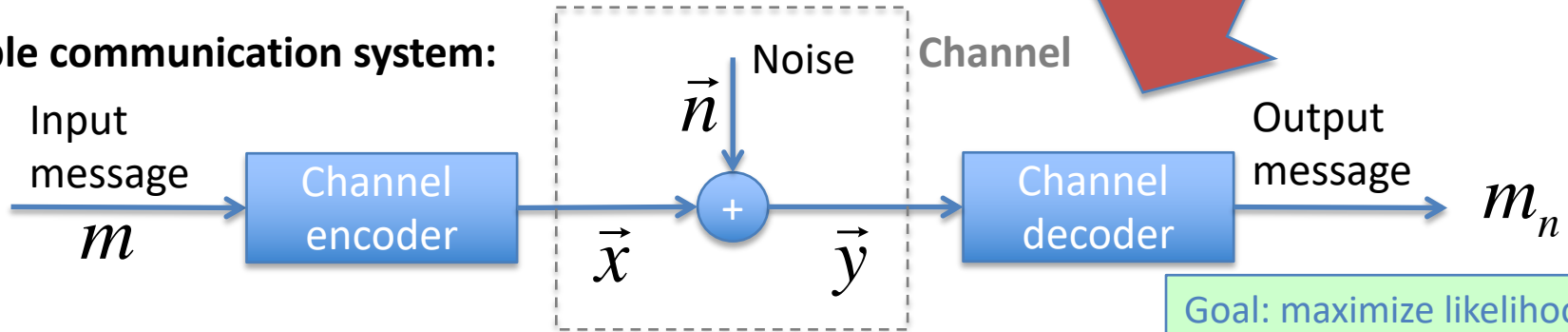
- **Embedding capacity:** maximum theoretically possible number of embedded bits
- **Steganographic capacity:** max payload hidden without artifacts, so that the detection is improbable
- **Embedding efficiency:** number of embedded bits per unit of distortion
- **Robustness against system / blind / targeted steganalysis**  
Based on method weakness (implementation fault, insufficient stego keyspace), statistical properties common to all methods, detectability of messages embedded with a specific method.
- **Statistical undetectability**  
Is it hard to notice the presence of a message? Usually (loosely!) quantified in terms of statistical anomalies, based on some statistical model of relevant Works.
- **False alarm rate:** tradeoffs characterized with Receiver Operating Characteristic (ROC) curves
- **Security:** resistance to passive (observation), active (obstruction), malicious (impersonation) attacks
- **Use of stego keys**  
Algorithm is assumed known, embedding is controlled by a secret key. Schemes can be symmetric or asymmetric; as a rule, key length does not influence the security as much as the length of crypto keys

# Small digression: communication systems

## Reminder: generic image compression + communication system



## Simple communication system:



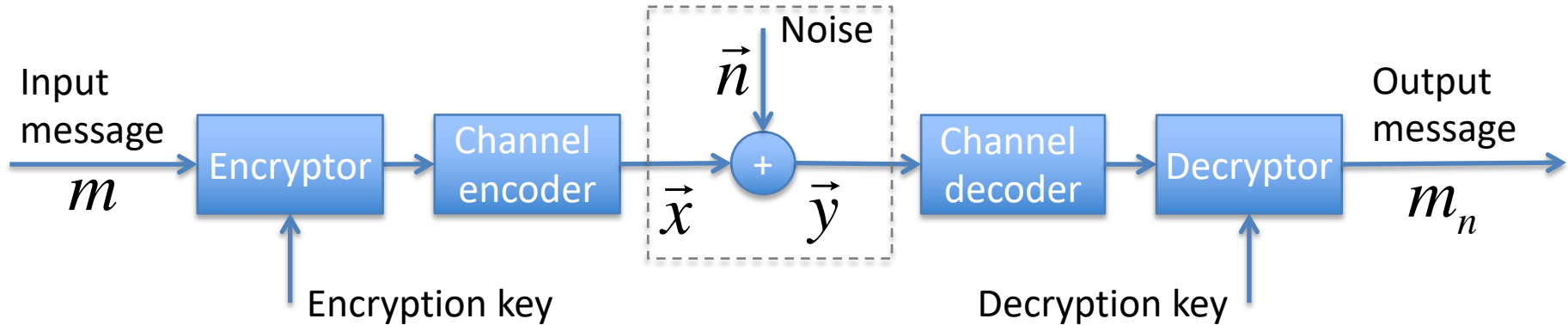
- Transmitted signal:  $\vec{x} = \{x_1, x_2, \dots, x_N\}$ ,  $\sum_i x_i^2 \leq p$

- Simplest channel: additive white Gaussian noise,  $\vec{y} = \vec{x} + \vec{n}, \vec{n} \sim N(\vec{0}, \sigma^2)$

Goal: maximize likelihood that the detected message is identical to the original

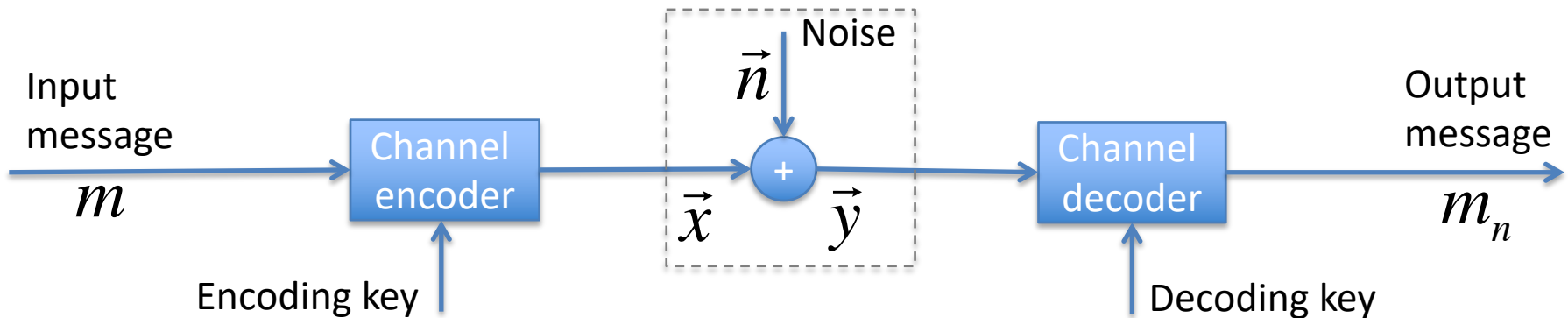
# Secure communication systems

## Communication with encryption:



Goal: secrecy of messages, messaging layer.  
Example: RSA encryption

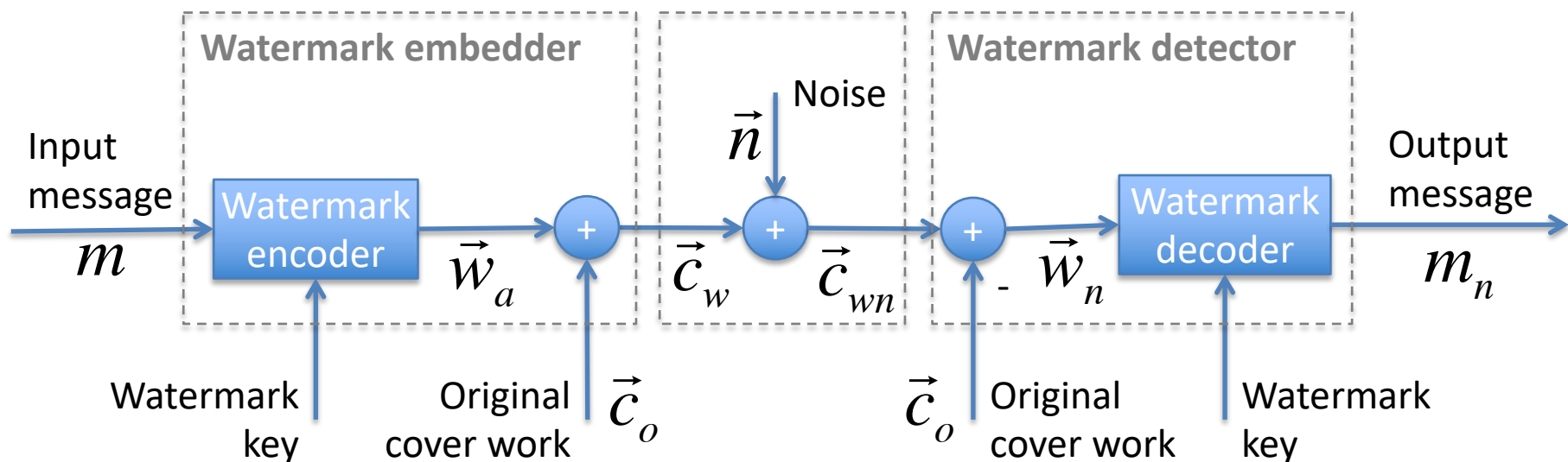
## Communication with key-based channel coding:



Goal: guaranteed delivery of signals, transport layer. Example: spread-spectrum radio

# Communication-based models of watermarking

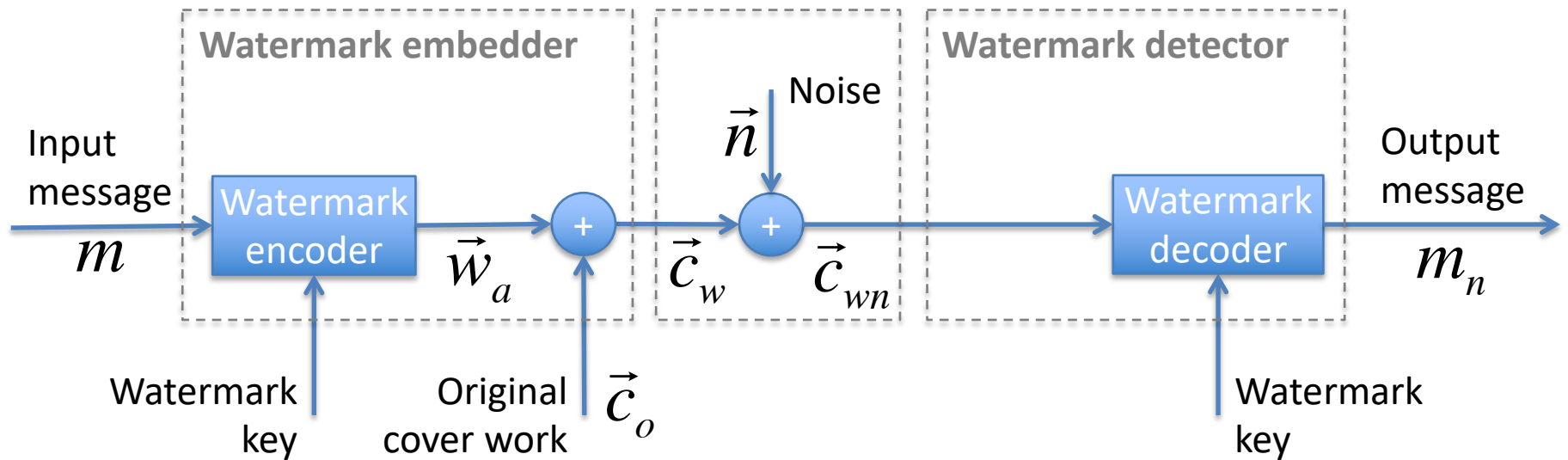
## Watermarking with a simple informed detector:



- Message mapped to *added pattern*  $w_a$  (could be via intermediate *message pattern*  $w_m$ )
- $w_a$  is added to cover work  $w_o$  to produce *watermarked work*  $c_w$  (i.e. blind embedder: ignores properties of cover work)
- Further processing adds noise  $n$  (could be more complex: compression, attacks etc.)
- If original work is subtracted, then the communication process is identical to simple communication model with additive noise

# Communication-based models of watermarking

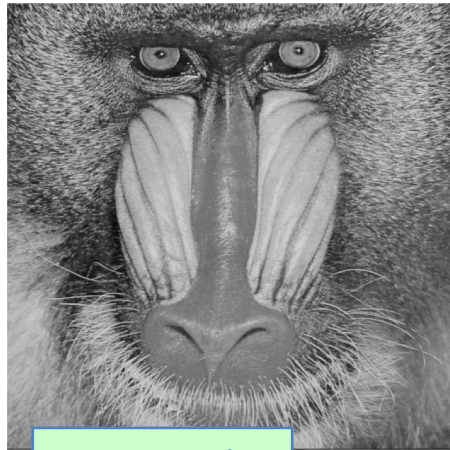
## Watermarking with a blind detector:



- In blind detector, cover work is just another kind of noise
- One goal: maximize similarity between the input and output messages
- Another possible goal: learn how exactly watermarked work was processed

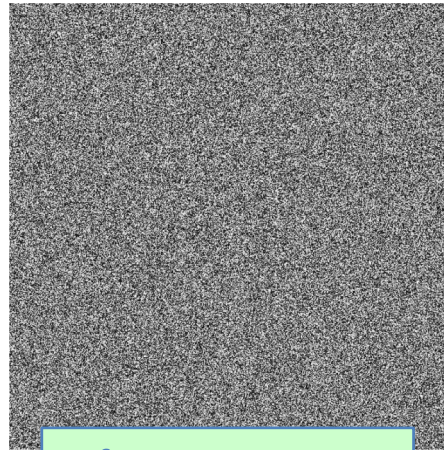
# Simple WM system: blind embedding, correlation detector

Embed **1-bit** message  $m$ :  $\vec{c} = \vec{c}_o + \alpha(2m - 1) \cdot \vec{w}_r$



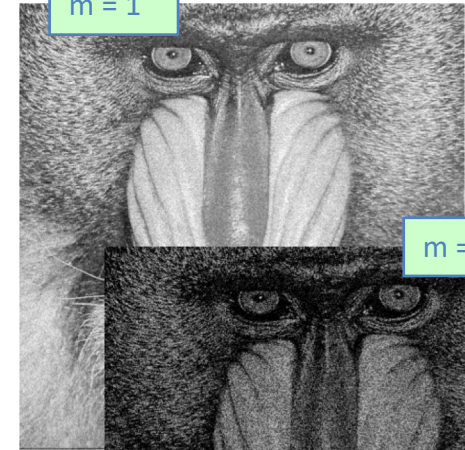
cover work

$+ \alpha(2m - 1) \cdot$

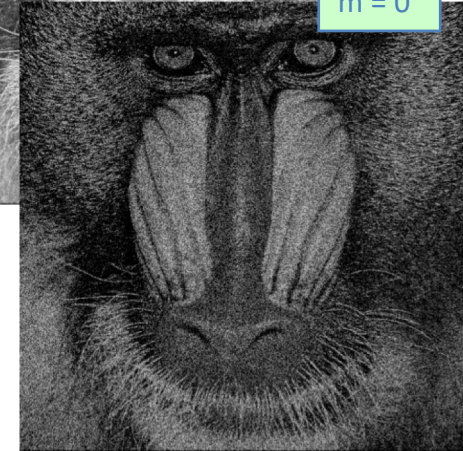


reference pattern

=



$m = 1$



$m = 0$

Detect message via **linear correlation** (scalar product):

$$z_{lc}(\vec{c}, \vec{w}_r) = \frac{1}{N} \vec{c} \cdot \vec{w}_r = \frac{1}{N} \sum_{x,y} c[x,y] \cdot w_r[x,y]$$

Effect from noise:

$$\vec{c} = \vec{c}_o \pm \alpha \cdot \vec{w}_r + \vec{n},$$

$$z_{lc}(\vec{c}, \vec{w}_r) = z_{lc}(\vec{c}_o, \vec{w}_r) + z_{lc}(\vec{n}, \vec{w}_r) \pm \alpha \cdot z_{lc}(\vec{w}_r, \vec{w}_r)$$

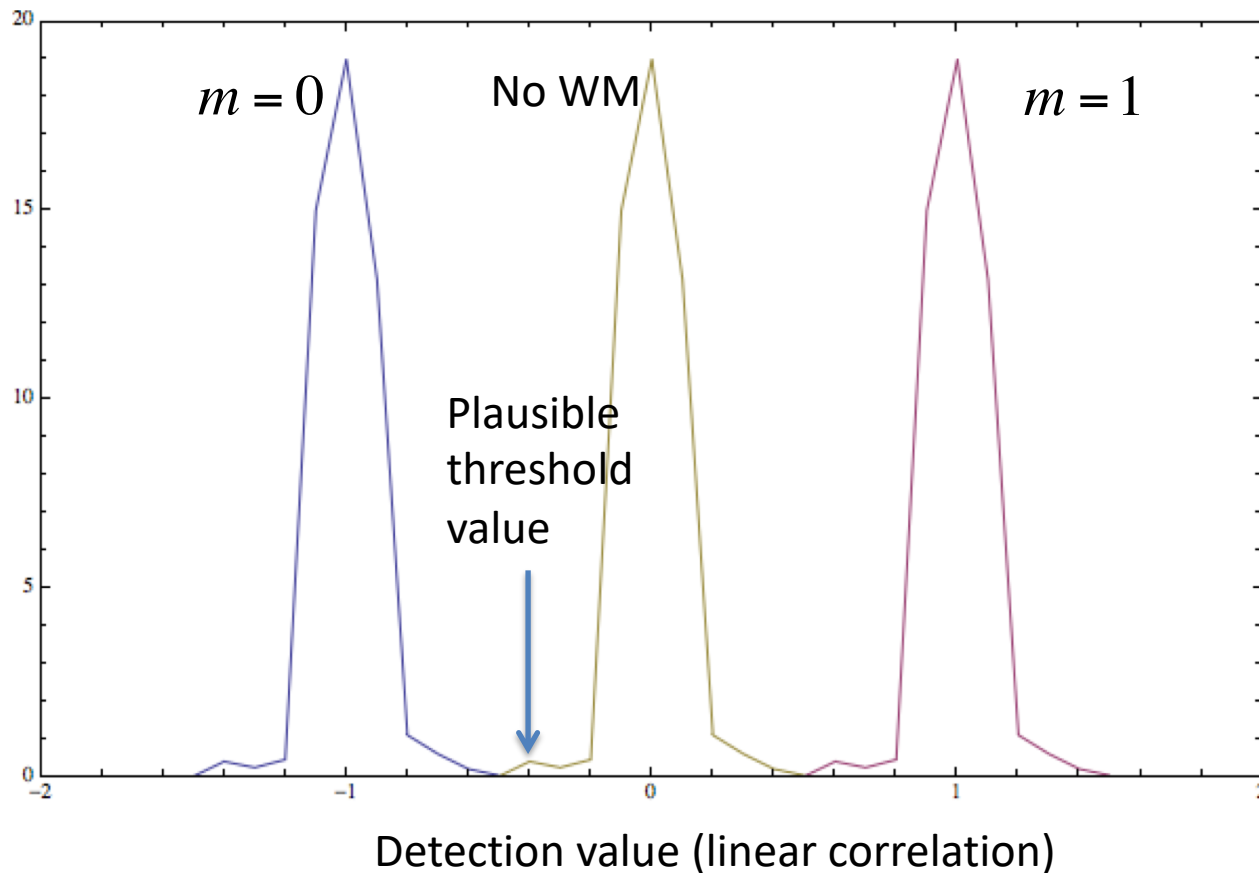
If reference pattern has zero mean, unit variance, then:

$$m_n = \begin{cases} 1, & z_{lc}(\vec{c}, \vec{w}_r) > \tau \\ no, & |z_{lc}(\vec{c}, \vec{w}_r)| < \tau \\ 0, & z_{lc}(\vec{c}, \vec{w}_r) < -\tau \end{cases}$$

# Testing simple WM system with DB of images

[Cox et al, '08]

Percentage of images

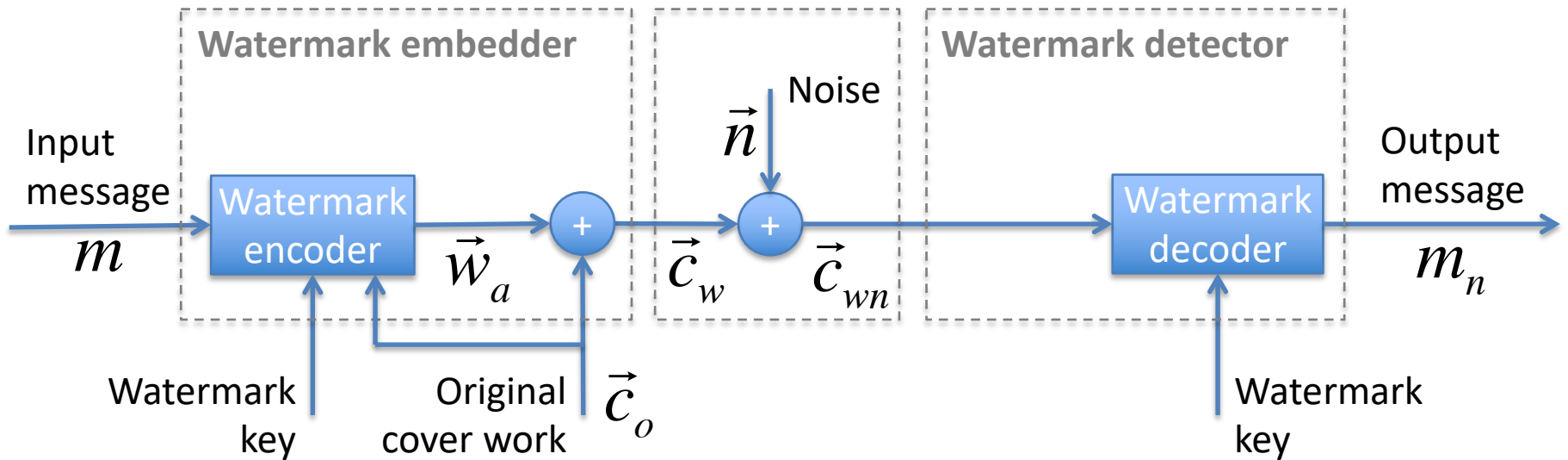


- DB of 4000 images
- Strength  $\alpha = 1$
- Threshold  $\tau = 0.7$  results in false positive probability of  $\sim 10^{-4}$
- Performance highly dependent on reference image!
- E.g. low-pass filtering results in much poorer separation, higher FP probability

Working and useful WM system; however, only optimal if the cover work and noise are drawn from Gaussian distribution, susceptible to certain attacks

# Watermarking as communication with side information

**Idea:** allow embedder to examine cover work before generating watermark



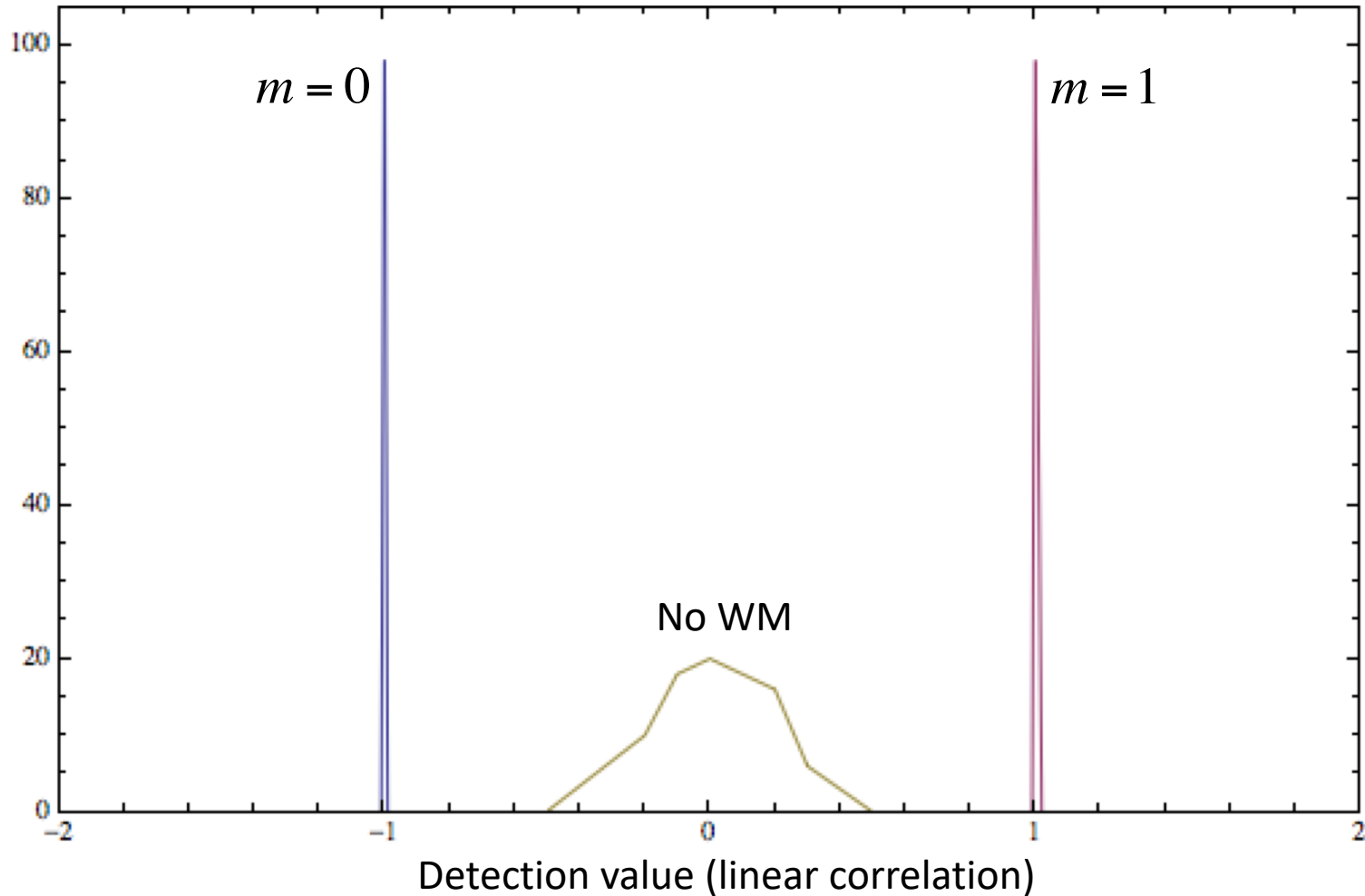
Can even subtract cover work completely!

- [Shannon, '58]: communication with side information at the transmitter
- Can modify embedder to guarantee 100% embedding efficiency (losing in fidelity)

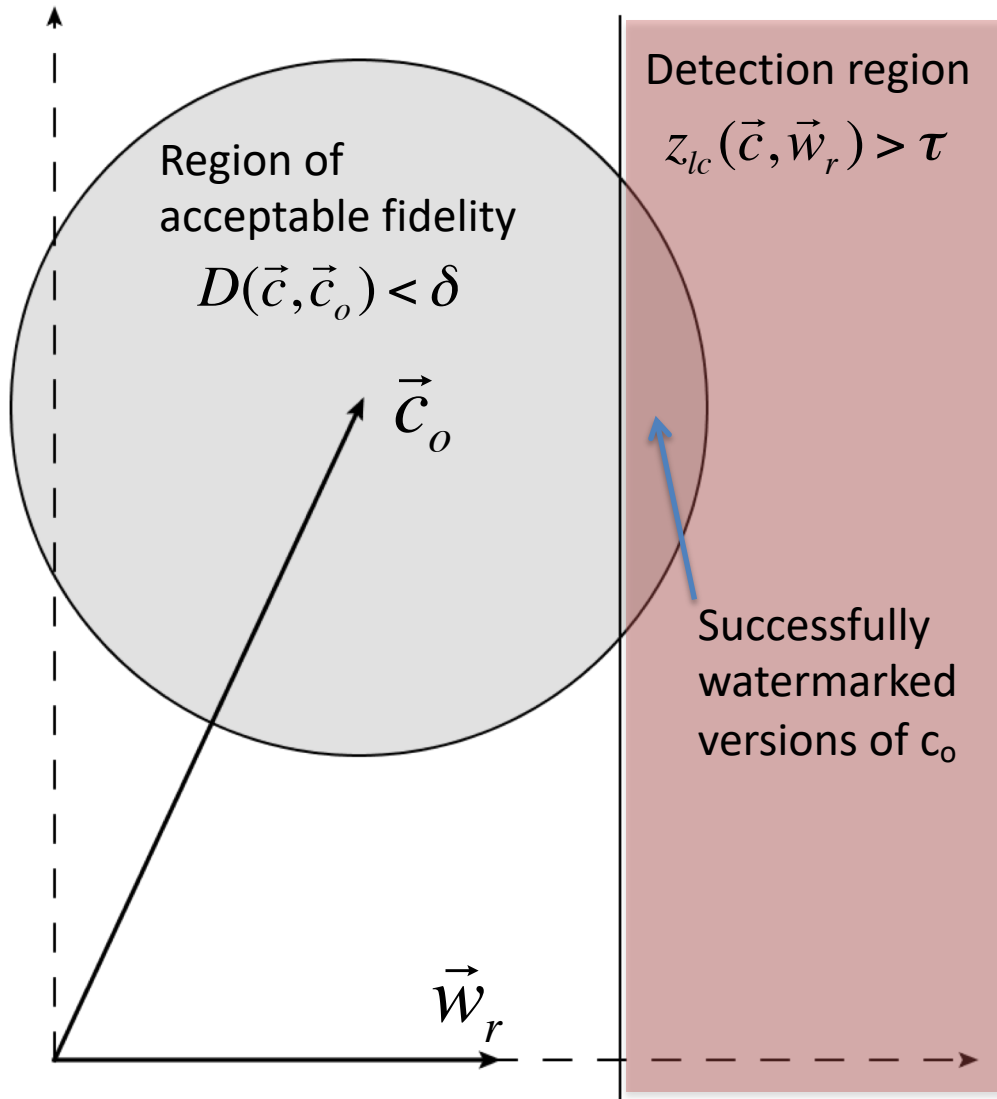
# Fixed correlation embedding

$$\vec{c} = \vec{c}_o + \alpha(2m-1) \cdot \vec{w}_r, \quad \alpha = \frac{\tau_{goal} - z_{lc}(\vec{c}_o, \vec{w}_r)}{z_{lc}(\vec{w}_r, \vec{w}_r)}$$

Percentage of images



**Media space:** multi-dimensional space of all works



Fidelity distance function extremely difficult to formalize; depends on human perception. Simplest case - MSE:

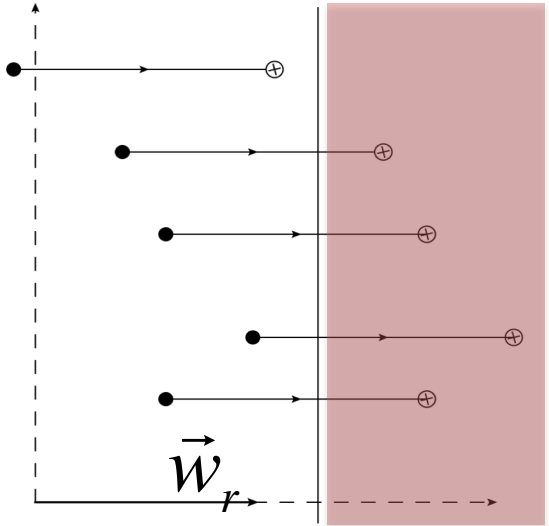
$$D_{MSE}(\vec{c}_1, \vec{c}_2) = \frac{1}{N} \|\vec{c}_1 - \vec{c}_2\|^2$$
$$= \frac{1}{N} \sum_{x,y} (c_1[x,y] - c_2[x,y])^2$$

Some perceptual distance functions are asymmetric, result in units of JND – just noticeable difference

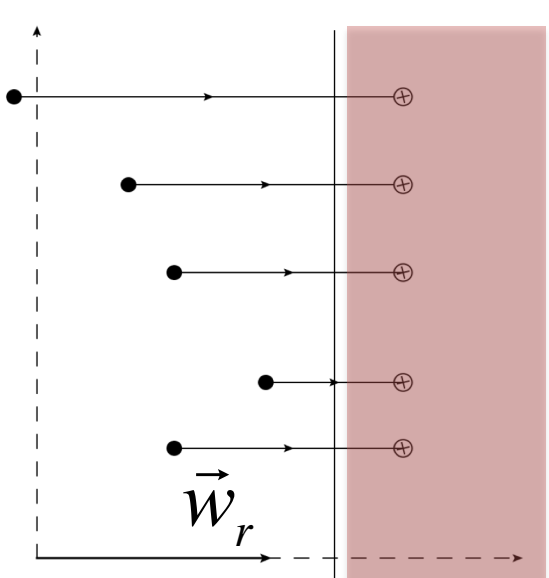
True distribution of works in media space is usually unknown, effect of transmission / noise / attacks also unknown 😊 (but modeled anyway)

# Effects of blind and fixed-correlation embedding

## Blind embedder



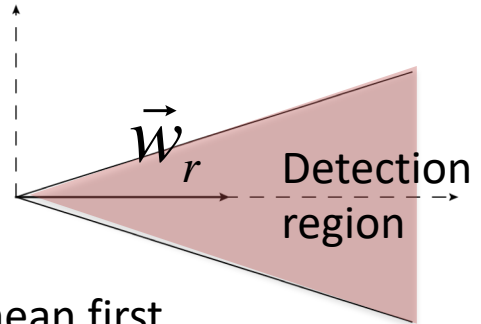
## Fixed-IC embedder



## Alternative common detection region definitions:

- Normalized correlation: angle in N-dim space

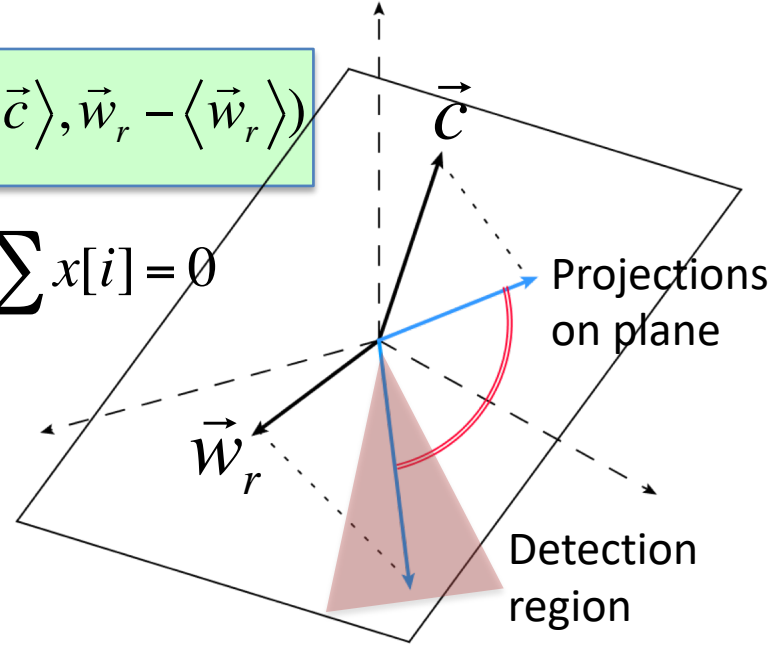
$$z_{nc}(\vec{c}, \vec{w}_r) = \frac{\vec{c} \cdot \vec{w}_r}{|\vec{c}| \cdot |\vec{w}_r|} = \cos(\angle(\vec{c}, \vec{w}_r))$$



- Correlation coefficient: subtract mean first (= angle between N-1-dimensional projections)

$$z_{cc}(\vec{c}, \vec{w}_r) = z_{nc}(\vec{c} - \langle \vec{c} \rangle, \vec{w}_r - \langle \vec{w}_r \rangle)$$

$$\text{Plane } \langle \vec{x} \rangle = \sum x[i] = 0$$



# Marking space (cf. transform-based compression)

- **Media space** (e.g. pixel values) not always convenient for watermarking
- **Extractor** transforms work to more convenient representation (e.g. frequencies, wavelets)
- Unlike image compression, not looking for more compact representation!

